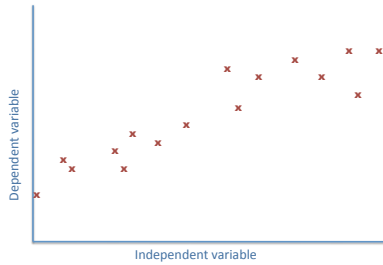
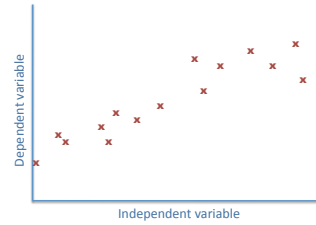


Evaluating Correlation or Association Regression Analysis



- Test: comparison of two variables (continuous data / one sample)

Example: continuous data / one sample / two variables



- Test: comparison of two variables:
– Correlation coefficient / linear regression

Pearson Sample Correlation Coefficient

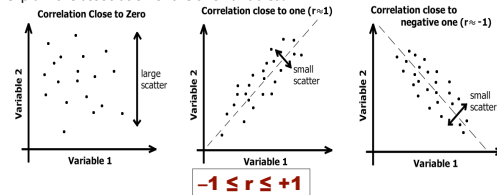
Does the Dependent variable correlate with the Independent variable?

$$r = \frac{n \sum xy - [(\sum x) (\sum y)]}{\sqrt{n (\sum x^2) - (\sum x)^2} \sqrt{n (\sum y^2) - (\sum y)^2}}$$

$$-1 \leq r \leq +1$$

Pearson Sample Correlation Coefficient

Does the Dependent variable correlate with the independent variable?
• How well does a linear regression (straight line) explain the association of the two variables?



- r is related to scatter (standard deviation) and slope
- If $r = 0$, y is not correlated with x (i.e., Δy is not associated with Δx)
- If $r > 0$, y (variable 2) is positively correlated with x (variable 1)
- If $r < 0$, y is negatively correlated with x

Is the Correlation Coefficient significantly different from 0?

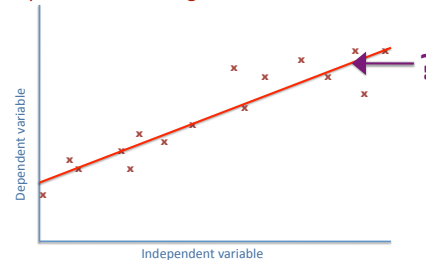
$$r = \frac{n \sum xy - [(\sum x) (\sum y)]}{\sqrt{n (\sum x^2) - (\sum x)^2} \sqrt{n (\sum y^2) - (\sum y)^2}}$$

- r is related to scatter (standard deviation) and slope
- If $r = 0$, y is not correlated with x (i.e., Δy is not associated with Δx)
- If $r > 0$, y (variable 2) is positively correlated with x (variable 1)
- If $r < 0$, y is negatively correlated with x

Compare $|r|$ with Critical Value for n .

Linear Regression

“Least Squares”: calculating the line that best fits the data



- Linear regression line
- Linear regression equation: $y = a + bx$
 - b = slope of the line ($\Delta y / \Delta x$)
 - a = y -intercept (value of y if $x=0$)

Least-Squares Line

- Exact equation for "line of best fit"

$$\hat{y} = a + bx$$

- Slope**, $b = \frac{n \sum xy - (\sum x)(\sum y)}{n \sum x^2 - (\sum x)^2}$
- Intercept**, $a = \bar{y} - b\bar{x}$
- Using standard deviation... $b = r \left(\frac{s_y}{s_x} \right)$
- (\bar{x}, \bar{y}) is on the least-squares line

Regression

Definition

❖ Regression Equation

Given a collection of paired data, the regression equation

$$\hat{y} = b_0 + b_1x$$

algebraically describes the **relationship** between the two variables

❖ Regression Line

(line of best fit or least-squares line)
is the graph of the regression equation

18

Least-Squares Regression Line

We can use technology to find the equation of the least-squares regression line. We can also write it in terms of the means and standard deviations of the two variables and their correlation.

Definition: Equation of the least-squares regression line

We have data on an explanatory variable x and a response variable y for n individuals. From the data, calculate the means and standard deviations of the two variables and their correlation. The least squares regression line is the line $\hat{y} = a + bx$ with

slope $b = r \frac{s_y}{s_x}$

and **y intercept** $a = \bar{y} - b\bar{x}$

Least-Squares Regression

Stats Chapter 5 - Least Squares Regression

Definition of a regression line:

A regression line is a straight line that describes how a response variable (y) changes as an explanatory variable (x) changes...

- Used to predict a y value given an x value.
- Requires an explanatory and a response variable.
- Given as an equation of a line in slope intercept form:

$$\hat{y} = a + bx$$

Read as: "y-hat" a = y-intercept b = slope

summary

- Regression equation: describes how a dependent variable (y) changes in association with an independent variable (x).
 - $y = a + bx$
 - a = y-intercept: the value of y when $x=0$.
 - b = slope: the rate at which y varies in association with x .
 - r = **correlation coefficient**: What is the probability that the change in y is related to the change in x ?
 - p-value: What is the probability that the change in y is **not** related to the change in x (H_0)?
 - r^2 = **determination coefficient**: *How much* (i.e., what fraction) of the variation in y is related to the variation in x ?
- Remember: correlation does not prove causation!

Scatterplots and Line-fitting in Excel

- <https://www.youtube.com/watch?v=Ohp1PpzrRhE>