

Instructions: Write complete legible solutions to the following problems in the space provided. Be sure to supply all the necessary steps that lead to your answers.

1. Evaluate the surface integral $\iint y \, ds$, where S is the helicoid with vector equation $\mathbf{r}(u, v) = \langle u \cos v, u \sin v, v \rangle$, $0 \leq u \leq 8$, $0 \leq v \leq \pi$.

2. Evaluate the surface integral $\iint_S x^2 y z \, dS$, where S is the part of the plane $z = 1 + 2x + 3y$, that lies above the rectangle $0 \leq x \leq 6$, $0 \leq y \leq 2$.

3. Evaluate the surface integral

$$\iint_C xz dS, \text{ where } S \text{ is the boundary of the region enclosed by the cylinder}$$
$$y^2 + z^2 = 9 \text{ and the planes } x = 0, \text{ and } x + y = 5$$

4. Evaluate the surface integral $\iint \mathbf{F} \cdot d\mathbf{S}$ for the given vector field \mathbf{F} and the oriented surface \mathbf{S} . In other words, find the flux of \mathbf{F} across \mathbf{S} .
 $\mathbf{F}(x, y, z) = xz\mathbf{i} + x\mathbf{j} + y\mathbf{k}$, and \mathbf{S} is the hemisphere $x^2 + y^2 + z^2 = 25, y \geq 0$ oriented in the direction of the positive y-axis.